

Basic Skills (4 points each)

1. Expand and simplify $(3 - 2\sqrt{5})^2$.

- A) $23 - 4\sqrt{5}$ B) $29 - 4\sqrt{5}$ C) $29 - 12\sqrt{5}$ D) $23 + 12\sqrt{5}$

2. Expand and simplify $(4 + i\sqrt{3})^2$

- A) $13 - 5i\sqrt{3}$ B) $19 + 8i\sqrt{3}$ C) $8 - 8i\sqrt{3}$ D) $13 + 8i\sqrt{3}$

3. $\log_2 \left(\frac{1}{16} \right)$ equals

- A) $1/4$ B) $-1/4$ C) 4 D) -4

4. Determine b if $\log_b (64) = -3$.

- A) $1/4$ B) $-1/4$ C) 4 D) -4

5. The vertical asymptotes of the graph of the rational function $f(x) = \frac{3x^2 + x - 1}{x^2 - 2x - 15}$ are

- A) $x = 3$ B) $x = 5, x = -2$ C) $x = -5, x = 2$ D) $x = 0, x = 15/2$

6. Convert 225° to radians.

- A) $7\pi/12$ B) $5\pi/4$ C) $5\pi/8$ D) $5\pi/12$

7. Convert $\frac{7\pi}{12}$ to degrees

- A) 105° B) 75° C) 210° D) 225°

8. $\sin(105^\circ)$ equals

- A) $\frac{\sqrt{6} + \sqrt{2}}{2}$ B) $\frac{\sqrt{6} + \sqrt{2}}{4}$ C) $\frac{\sqrt{6} - \sqrt{2}}{2}$ D) $\frac{\sqrt{6} - \sqrt{2}}{4}$

9. $\sec \left(\tan^{-1} \left(\frac{7}{12} \right) \right)$ in $[0, \pi/2]$ equals

- A) $\frac{5}{12}$ B) $\frac{\sqrt{193}}{12}$ C) $\frac{\sqrt{95}}{7}$ D) $\frac{\sqrt{193}}{12}$

10. $\cos \left(\sin^{-1} \left(\frac{4}{9} \right) \right)$ in $[\pi/2, \pi]$ equals

- A) $-\frac{\sqrt{5}}{9}$ B) $-\frac{\sqrt{65}}{9}$ C) $\frac{9}{\sqrt{97}}$ D) $-\frac{9}{\sqrt{97}}$

11. Change $\left(8, \frac{\pi}{6} \right)$ from polar coordinates to rectangular coordinates.

- A) $(4, 4\sqrt{3})$ B) $(8, 8\sqrt{3})$ C) $(4\sqrt{3}, 4)$ D) $(4, 4\sqrt{3})$

12. Change $(-6, 6)$ from rectangular coordinates to polar coordinates.

- A) $(6, \pi/4)$ B) $(6\sqrt{2}, 3\pi/4)$ C) $(6, 3\pi/4)$ D) $(-6\sqrt{2}, 5\pi/4)$

13. If $\mathbf{u}=(-3, 2)$ and $\mathbf{v}=(4, 5)$, then $3\mathbf{u}+4\mathbf{v}$ equals

- A) $(25, 26)$ B) -24 C) $(7, 26)$ D) $(-7, 26)$

14. If $\mathbf{w}=(4, 9)$, then $|\mathbf{w}|$ equals

- A) 13 B) $\sqrt{65}$ C) 5 D) $\sqrt{97}$

15. Match the given equation with the type of conic:

_____ $x^2 + 3y^2 = 8$

A. CIRCLE

_____ $y = 3(x - 1)^2 + 2$

B. ELLIPSE

_____ $3x^2 - y^2 = 1$

C. PARABOLA

_____ $x^2 + (y - 1)^2 = 8$

D. HYPERBOLA

More Skills (Non-multiple choice - 5 points each)

16. In the triangle ABC, $\angle A = 30^\circ$, $\angle B = 45^\circ$, $A=32$. Determine B.

17. In the triangle ABC, $A=10$, $B=8$, $\angle C = 60^\circ$. Determine C.

18. If $\mathbf{u}=(b, 5)$ and $\mathbf{v}=(b, -2)$, determine b so that the vectors \mathbf{u} and \mathbf{v} are perpendicular.

19. Determine the equation of the line which passes through the point $P(2, 40)$ and is perpendicular to $x + 2y = 8$.

20. If $\ln(a) = 1.5$, $\ln(b) = 6$, and $\ln(c) = -2$, determine $\ln\left(\frac{ab^2}{\sqrt{c}}\right)$

21. Write as a single logarithm $2\ln(3) - 5\ln(2) + 6\ln(1)$

22. If vector $\mathbf{u}=(2, 3)$ and vector $\mathbf{v}=(5, 1)$, determine the angle between them.

23. If $f(x) = x^2 - 3x + 5$ determine $\frac{f(2+h) - f(2)}{h}$ and simplify as much as possible.

The following questions are worth 10 points each

24. Give the inverse of the function $f(x) = \frac{2x + 1}{4x - 7}$

25. Give the inverse of the function $f(x) = 5 \ln\left(\frac{x - 1}{2}\right)$

26. Give the center and radius of the circle $x^2 + y^2 + 6x - 5y + 3 = 0$

27. (8 pts) Divide and give the quotient in the space provided.

$$\begin{array}{r} 3x^4 + 2x^3 - x^2 + 4x - 68 \\ \hline x - 2 \end{array}$$

28. \$1000 is deposited at 6% annual interest compounded semi-annually, (twice a year).
In how many years will the investment double? (Leave your answer as $t =$)

29. If $\sin \theta = \frac{4}{9}$ and $\frac{\pi}{2} \leq x \leq \pi$, determine:

(a) $\sin(2\theta) = \underline{\hspace{2cm}}$

(b) $\cos(2\theta) = \underline{\hspace{2cm}}$

30. Sketch the graph of $y = 5 + 10 \cos\left(\frac{\pi x}{2}\right)$. Label each x -intercept and label each of the points (x, y) where the function reaches its highest and lowest values.

31. Solve $\log_2(x) + \log_2(x + 6) = 4$

32. If $f(x) = 2x^2 - 5x - 3$, determine the vertex and x -intercepts.

vertex = _____

x -intercepts = _____

33. Determine the exact value of $z = (2 + 2i)^4$