We investigate the problem of the Lévy flight foraging hypothesis both in an ecological niche described by a bounded region of space and in the whole \mathbb{R}^n .

To this end, we consider a forager diffusing according to a suitable fractional heat equation and we define several efficiency functionals whose optimality is discussed in relation to the fractional exponent $s \in (0, 1)$ of the diffusive equation.

We analyze the biological scenarios in which a target is close to the forager or far from it. In particular, for all the efficiency functionals considered here, we show that if the target is either close or far enough to the forager, then the most rewarding search strategy will be in a small neighborhood of s = 0.

Interestingly, we show that s = 0 is a global pessimizer for some of the efficiency functionals. From this, together with the aforementioned optimality results, we deduce that the most rewarding strategy can be unsafe or unreliable in practice, given its proximity with the pessimizing exponent, thus the forager may opt for a less performant, but safer, hunting method.

However, the biological literature has already collected several pieces of evidence of foragers diffusing with very low Lévy exponents, often in relation with a high energetic content of the prey. It is thereby suggestive to relate these patterns, which are induced by distributions with a very fat tail, with a highrisk/high-gain strategy, in which the forager adopts a potentially very profitable, but also potentially completely unrewarding, strategy due to the high value of the possible outcome.